

The Definition of the Parameters of Superconducting Film for Production of Protection Equipment Against Electromagnetic Environmental Effects

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Abstract — The paper presents the results of evaluating the propagation of a plane electromagnetic wave (EMW) over the surface of a film made of a high-temperature superconductor (HTS) in both superconducting S and normal N states, as well as an analysis of the parameters of a thin HTS film necessary for implementing a device for protection against electromagnetic radiation. Evaluation of the propagation of EMW over the surface of a thin HTS film was performed on the basis of a two-fluid model. As a result of the research, relations were obtained for determining the value of the surface impedance and the depth of penetration of EMW into a superconducting film in S and N states. It is shown that the expression for determining the penetration depth of EMW into a superconducting film in the normal N state is applicable provided that the frequency of the signal field does not exceed the critical value, which is determined by the binding energy of charge carriers at a temperature not exceeding the transition temperature to the superconducting state. Based on the relations for determining the surface impedance of a thin HTS film, relations are obtained for the active surface resistance, which is the real part of the surface impedance, and the surface reactance, which is its imaginary part, in the superconducting and normal states. Using these ratios, the quality parameter of the HTS thin film is introduced. The dependence of the quality factor of the HTS film on its thickness is found. It is shown that the highest value of the quality factor is realized when the film thickness is less than or of the order of the penetration depth. It is noted that this dependence is valid only if the film thickness does not depend on its quality.

Keywords — superconducting film, electromagnetic wave, two-fluid model, surface impedance, penetration depth.

I. INTRODUCTION

The intensive development and application of powerful generation systems makes it necessary to find the most effective means of protecting telecommunication, communication and navigation systems, ground survey systems that may be disrupted by high-intensity electromagnetic pulse radiation (EMR) and ultra-short pulse duration [1]. In the articles [2, 3] the ways and means of protection of radio-electronic devices based on the application of construction materials and nature-like technologies are considered. The articles [4, 5] on high-speed protective devices discuss the use of thin superconducting films. The construction of protective devices based on high-temperature superconductors (HTS) depends on the possibility of carrying out reversible S-N phase transitions therein. A typical representative of HTS is the $YBaCuO_{7-x}$ compound, which is a type II superconductor. In such HTS, the surface energy at the edge between superconducting and normal phases is negative when forming a normal area in superconducting state. This results in the instability of the type II superconductors in relation to the formation of vortices (Abrikosov vortices), each of which carries a magnetic flux quantum.

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Instability occurs in the lower critical field, where vortices are considered at distances of the depth of penetration of the field into the superconductor. When the normal areas of vortices are closed, the superconducting state is destroyed. External inputs may disrupt the superconductivity of the HTS and consequently the state of normal regions. Thus, the determination of the appropriateness of using HTS for the creation of devices for the protection of radio electronic means against pulsed EMR makes it necessary to carry out studies aimed at studying the destruction of superconducting state under external influences, as well as definition of parameters of superconducting film at which switch conditions will be implemented.

II. ANALYSIS OF LITERATURE DATA AND PROBLEM STATEMENT

The article [6] considers the use of HTS as adjustable filters under the influence of an electric field. The authors limited themselves to studying the frequency properties of such filters. In particular, they showed that with a DC voltage bias, it is possible to provide filter tuning at about 2.5 GHz with a bandwidth of less than 2% and more than 15% of the adaptive range. The change in the state of superconductivity under external influence was not considered in the work.

The article [7] shows the possibility of creating controllable filters and amplifiers, the design of which includes a thin HTS film in a mixed state. Amplification of EMW occurs as a result of the interaction of a wave with a magnetic vortex grid moving in the superconductor film. Attenuation or amplification is controlled by changing the magnetic field. However, the implementation of EMR protection devices is not affected. HTS applications for narrowband filters and resonators have been studied in a number of papers [8-11].

In [8], based on the method of moments, a technique for designing a filter with a fractional passband of 2.27% at a frequency of 883.0 MHz is proposed. The filter is made using thin films of thallium-barium-calcium-copper oxide on a two-inch plate of lanthanum aluminate (LaAlO₃). The S-parameters of the filter are investigated, good agreement with the simulation results is shown. The use of superconducting thin films based on LaAlO₃ in protective devices was not considered in this work. In [9], the results of studies of 10-pole microstrip bandpass filters with a central frequency of 1.75 GHz are presented.

The high performance of the filter with an insertion loss of no more than 0.5 dB and the ability to control the power up to 10 W of the input power at T = 60 K is shown. The possibility of changing the state of superconductivity of a microstrip line under the influence of an external electromagnetic field has not been studied.

In [10], intermodulation distortions were investigated when signals are applied at more than one frequency. In [11], the results of studies of the design and operational characteristics of coplanar waveguide microwave filters using superconducting films are presented. The results of experimental studies of a prototype of a miniature CPW filter with its simulated characteristics are presented.

In [12], the results of the development of a high-temperature superconducting receiving filter with a narrow passband characteristic of a 9 GHz weather radar are presented to reduce interference between adjacent radar channels. To suppress radiation losses and achieve a high Q-factor, coupled microstrip linear resonators with a wavelength of 1.5 times and a resonant frequency of an odd mode were used. The frequency response of the filter at the center frequency of 9700 MHz has an insertion loss of 1.8 dB, which is consistent with the design specifications. The use of HTS for the implementation of the protection device has not been considered.

In [13], the design and modeling of the UWB filter characteristics are considered. The proposed UWB filter provides huge bandwidth from 2.5 GHz to 8 GHz. Filter estimation parameters such as return loss, insertion loss, phase and group delay are obtained and their responses analyzed. The filter return loss (S₁₁) and insertion loss (S₂₁) are shown to be -40 dB and -1 dB, respectively. The use of an EMR filter has not been considered.

In [14], a compact coplanar waveguide dual-band high-temperature superconducting band-pass filter with a dummy short-circuited ring resonator (SC-SLRR) is presented. The relationship between the parameters of electrical length and resonance characteristics is shown. The authors limited themselves to studying only the frequency properties of the filter.

In [15], a compact band-pass filter based on multimodal coplanar waveguide resonators implemented using a slow-wave periodic structure is presented. A multimodal circuit model of the filter is proposed and experimentally confirmed. A prototype second order filter at 1.9 GHz with a compact size of 0.31 λ_g x 0.19 λ_g was developed and manufactured. The filter has measured fractional passbands of 9.3% and 3.7% for rejection levels of 20 and 30 dB, respectively, and 1.3 dB insertion loss in passband.

Geometric models of broadband circuits for various configurations of a loaded slot line and loaded coplanar waveguide (CPW) are presented in [16]. Also presented are three applications, the design of which is based on the proposed modeling methodology. It is a maximally flat third-order low-pass filter with a cutoff frequency of 1.4 GHz, a slow-wave structure of 3 GHz with a slow-wave ratio greater than 2 in the linear range of the dispersion ratio, and a balanced composite right / left SRR-loaded CPW with 100% (2.31-7,1 GHz) fractional bandwidth.

The paper [17] suggests an electrodynamic model describing the dispersion properties of the magnetostatic surface wave in the structure of the ferrite/superconductor, on the basis of which the surface resistance of the superconducting film in the magnetic field is determined. However, the destruction of the superconducting state by EMW propagating along the HTS has not been investigated. The work [18] contains the results of the analysis of the frequency dependence of the penetration depth of the magnetic field into the conductor, assuming that the pseudo-alkali phase is related to the charge density waves. The dissemination of EMW along the HTS was not addressed. Also, changes in surface resistance due to EMW exposure were not estimated. Thus, in the well-known studies of the use of HTS in the creation of microwave components, the study of the destruction of superconducting states under external influences, as well as the determination of superconducting film parameters, where switching conditions will be implemented has not been properly developed.

The aim of the article is to determine the conditions for the transition of a thin HTS film from the superconducting state to the normal state under external influence, as well as the parameters of the superconducting film under which the switching conditions will be realized.

In order to achieve the object of the research, the following tasks have to be accomplished.

1. Estimate the effect of EMW propagating over the surface of a thin HTS film on its transition from a superconducting state to a normal state.
2. Perform an analysis of the HTS parameters necessary for the implementation of the EMR protection device.

III. MAIN MATERIAL

1) Evaluation of the effect of EMW spreading over the surface of the thin HTS on its transition from a superconducting state to a normal state.

If an EMW propagates in a dielectric and falls on the surface of a superconducting film in the S or N state, the wave reflectance will be close to 1 [19] with the electromagnetic field of the wave partially penetrating the conductor, and some of the energy turns to heat. The penetration depth of the magnetic field into the superconductor and the surface impedance are quantitative characteristics that describe the phenomena occurring in the superconducting strip.

Most commonly, when solving the problems of technical electrodynamics, HTS is considered as the ideal conductor. In this case the penetration depth and the surface impedance are zero, the incident wave is reflected completely, the field is not penetrated into the conductor, the energy of the wave is not absorbed. However, no perfect conductors exist. It is known that as the frequency of the electromagnetic field increases, the penetration depth and surface impedance increase. Therefore, in order to create a protective device based on HTS, we shall carry out a study of the spread of a flat electromagnetic wave over the surface of a film made of HTS, both in the S and N states.

The penetration of the electromagnetic wave into the HTS film located on the dielectric substrate is considered on the basis of the two-fluid model [20]. The essence of the model is that all charge carriers in the material are divided into two groups: charge carriers in a normal state with n_N concentration, and charge carriers in a superconducting state with n_S concentration.

The total concentration of charge carriers n equals to:

$$n = n_S + n_N. \quad (1)$$

Let's suppose a time-variable electric field with tension \vec{E} in a superconductor.

Then for superconducting film in superconducting state, let's form first London equation [20]:

$$\frac{\partial \vec{j}_S}{\partial t} = \frac{1}{\Lambda} \vec{E}, \quad (2)$$

where $\Lambda = \frac{m_s}{n_s e^2}$,

m_s - effective mass of superconducting charge carriers;
 n_s - superconducting electron concentration;
 e - electron charge.

According to the two-fluid model, the current density of the superconducting charge carriers is related to their motion speed.

Therefore, equation (2) can be rewritten as:

$$\bar{j}_s = en_s \bar{v}_s, \quad (3)$$

where $\frac{\partial \bar{v}_s}{\partial t} = \frac{e}{m_s} \bar{E}$.

To determine the current density, let's record the expression for the speed of superconducting charge carriers and the first Maxwell's equations:

$$\begin{cases} \frac{\partial \bar{v}_s}{\partial t} = \frac{e}{m_s} \bar{E}, \\ \text{rot } \bar{H} = \sigma_N \bar{E}, \end{cases} \quad (4)$$

where σ_N is the specific conductivity of the HTS in the N-state.

The density of current flowing through the superconducting film is known to vary mainly with respect to the width of the strip.

Then equations (4) in the rectangular reference system (fig. 1) can be written as follows:

$$\begin{cases} \frac{\partial v_{sx}}{\partial t} = \frac{e}{m_s} E_x, \\ \frac{\partial H_z}{\partial y} - \frac{\partial H_y}{\partial z} = \sigma_N E_x, \\ \frac{\partial H_x}{\partial z} - \frac{\partial H_z}{\partial y} = \sigma_N E_y, \\ \frac{\partial H_y}{\partial x} - \frac{\partial H_x}{\partial y} = \sigma_N E_z. \end{cases} \quad (5)$$

For a flat electromagnetic wave \bar{E} and \bar{H} don't depend on x and y (see fig. 1), but only on z and t .

Therefore, $\frac{\partial H}{\partial x} = 0$, $\frac{\partial H}{\partial y} = 0$, $H_x = 0$

Then equations (5) can be rewritten as:

$$\begin{cases} \frac{\partial v_{sx}}{\partial t} = \frac{e}{m_s} E_x, \\ \frac{\partial H_y}{\partial z} = \sigma_N E_x. \end{cases} \quad (6)$$

or

$$-\frac{e}{m_s \sigma_N} \frac{\partial H_y}{\partial z} = \frac{\partial v_{sx}}{\partial t}. \quad (7)$$

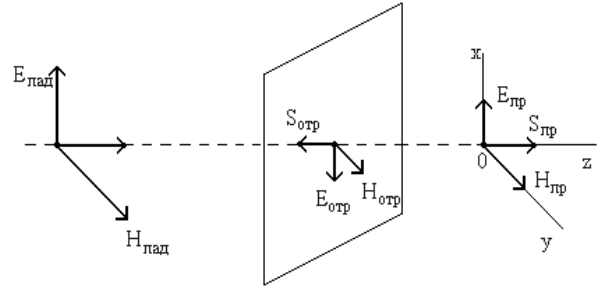


Fig. 1 Penetration of flat electromagnetic wave into the superconducting film

Assume that the electrical and magnetic field stresses change according to sinusoidal law:

$$\begin{cases} E_x = E_m \sin(\omega t + \varphi_1), \\ H_y = H_m \sin(\omega t + \varphi_2), \end{cases} \quad (8)$$

Where φ_1 and φ_2 are the initial phases.

Then the change in the current density and speed of the superconducting charge carriers is proportional to the change in the intensity of the electric field:

$$\begin{cases} v_{sx} = v_{sm} \sin(\omega t + f_1), \\ H_y = H_m \sin(\omega t + f_2). \end{cases} \quad (9)$$

By presenting the expressions (9) in an indicative form and placing them in equation (7), we have:

$$-\frac{e}{m_s \sigma_N} \frac{d\dot{H}_m}{dz} = i\omega \dot{V}_{s_m}, \quad (10)$$

or

$$\dot{V}_{s_m} = i \frac{e}{m_s \sigma_N \omega} \frac{d\dot{H}_m}{dz}. \quad (11)$$

The current density of the superconducting charge carriers can then be written as follows:

$$\dot{j}_s = i \frac{e^2 n_s}{m_s \sigma_N \omega} \frac{d\dot{H}_m}{dz},$$

Or

$$\dot{j}_s = -i \frac{1}{\omega \mu_0 \lambda_1^2} \dot{E}_m, \quad (12)$$

Where $\lambda_1^2 = \frac{m_s}{n_s e^2 \mu_0}$ is the London penetration depth;

μ_0 - magnetic constant.

For charge carriers in the normal state, the current density j_N can be written based on the first Maxwell equation:

$$\dot{j}_N = \sigma_N \dot{E}_m. \quad (13)$$

The expressions (12), (13) for j_N and j_s are valid for local current-field communication.

To describe the propagation of the wave in a superconducting film, determine the wave resistance Z .

For a wave in a vacuum:

$$Z_0 = \sqrt{\frac{\mu_0}{\epsilon_0}}. \quad (14)$$

In addition to the conductivity currents j_s and j_N , there is an offset current $i\omega \epsilon_0 \epsilon_{cp} \dot{E}_m$ determined by the dielectric permeability of the medium ϵ_{cp} .

The sum of currents (full current) makes it possible to obtain the effective dielectric permeability of the medium:

$$\epsilon_{\text{eff}} = \epsilon_0 \epsilon_{cp} \frac{\sigma}{i\omega} - \frac{1}{\omega^2 \mu_0 \lambda_1^2}. \quad (15)$$

Taking into account (14) we shall have:

$$Z = \frac{i\omega \mu_0}{\sqrt{\lambda_1^{-2} + i\omega \mu_0 \sigma_N}}, \quad (16)$$

where ω_0 is the EMR frequency.

It is clear that the complex penetration depth is defined as:

$$\delta^{-2} = \lambda_1^{-2} + i\omega \mu_0 \sigma_N. \quad (17)$$

Let's rewrite the expression (16) as follows:

$$Z = \frac{i\omega \mu_0 \lambda_1}{\sqrt{\left(1 + \frac{\lambda_1^2}{\delta_{sk}^2} i\right)^2 + \frac{\lambda_1^4}{\delta_{sk}^4}}}, \quad (18)$$

where $\delta_{sk} = \sqrt{\frac{2}{\omega \mu_0 \sigma_N}}$ is the depth of the skin layer.

At $T < T_c$ (where T_c is the temperature of transition into superconducting state) the condition [7] is generally met:

$$\lambda_1 \ll \delta_{sk}, \quad (19)$$

which allows to get the next simple result:

$$Z = \frac{1}{2} (\omega \mu_0)^2 \lambda_1^3 \sigma_N + i\omega \mu_0 \lambda_1. \quad (20)$$

At $T > T_c$, the strip has only normal conductivity.

Then the basic equations of the electromagnetic field can be written as:

$$\begin{cases} \text{rot } \bar{H} = \sigma_N \bar{E}, \\ \text{rot } \bar{E} = -\mu_0 \frac{\partial \bar{H}}{\partial t}. \end{cases} \quad (21)$$

As with superconducting states, let us consider the case where a flat EMW, propagating in dielectric, comes normally to a flat surface restricting superconducting film on one side.

Suppose that both media extend from the partition surface to infinity.

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The incident wave is partly reflected off the superconductor surface, partially penetrated and absorbed into it (see fig. 1).

For a rectangular coordinate system of equation (21) can be written as:

$$\left\{ \begin{array}{l} \frac{\partial H_z}{\partial y} - \frac{\partial H_y}{\partial z} = \sigma_N E_x, \\ \frac{\partial H_x}{\partial z} - \frac{\partial H_z}{\partial y} = \sigma_N E_y, \\ \frac{\partial H_y}{\partial x} - \frac{\partial H_x}{\partial y} = \sigma_N E_z, \\ \frac{\partial E_z}{\partial y} - \frac{\partial E_y}{\partial z} = -\mu_0 \frac{\partial H_x}{\partial t}, \\ \frac{\partial E_x}{\partial z} - \frac{\partial E_z}{\partial x} = -\mu_0 \frac{\partial H_y}{\partial t}, \\ \frac{\partial E_y}{\partial x} - \frac{\partial E_x}{\partial y} = -\mu_0 \frac{\partial H_z}{\partial t}. \end{array} \right. \quad (22)$$

For flat EMW \bar{E} and \bar{H} do not depend on x and y (see fig. 1), but only on z and t.

On that basis we shall record:

$$\frac{\partial H}{\partial x} = 0, \frac{\partial H}{\partial y} = 0, \frac{\partial E}{\partial x} = 0, \frac{\partial E}{\partial y} = 0, H_x = 0.$$

Then equations (22) can be rewritten as:

$$\left\{ \begin{array}{l} -\frac{\partial H_y}{\partial z} = \sigma_N E_x, \\ \frac{\partial E_x}{\partial z} = -\mu_0 \frac{\partial H_y}{\partial t}. \end{array} \right. \quad (23)$$

Equations (23) define EMW in a superconducting film in a normal state.

Assume that the electrical and magnetic field stresses change according to sinusoidal law:

$$\left\{ \begin{array}{l} E_x = E_m \sin(\omega t + \varphi_1), \\ H_y = H_m \sin(\omega t + \varphi_2). \end{array} \right. \quad (24)$$

By presenting the expressions (24) in a representative form in equation (22) and by making a reduction by a total multiplier $e^{i\omega t}$, we obtain:

$$\left\{ \begin{array}{l} -\frac{d \dot{H}_m}{dz} = \sigma_N \dot{E}_m, \\ \frac{d \dot{E}_m}{dz} = i\omega \mu_0 \dot{H}_m. \end{array} \right. \quad (25)$$

By differentiating the first equation in (25) by z and applying to the right of the obtained equation a value from the second equation is obtained:

$$\frac{d^2 \dot{H}_m}{dz^2} = i\omega \mu_0 \dot{H}_m. \quad (26)$$

Equality (26) is a second-order linear differential equation with a constant coefficient whose solution is:

$$\dot{H}_m = A_1 e^{-pz} + A_2 e^{pz}, \quad (27)$$

where A_1 and A_2 are permanent integrations;

$$p = \sqrt{i\omega \mu_0 \sigma_N}. \quad (28)$$

Considering that $\sqrt{i} = \frac{1}{\sqrt{2}}(1+i)$, the expression (28) can be rewritten as:

$$p = \sqrt{i\omega \mu_0 \sigma_N} = (1+i) \sqrt{\frac{\omega \mu_0 \sigma_N}{2}}. \quad (29)$$

A permanent integration of A_2 can be defined for the following reasons.

If $A_2 \neq 0$, then with the growth of z, as seen in the expression (27), \dot{H}_m must increase to infinity.

Since \dot{H}_m cannot grow to infinity when EMW is distributed, then, therefore, for physical reasons, there must be $A_2 = 0$.

Then:

$$\dot{H}_m = A_1 e^{-pz}. \quad (30)$$

The integration constant A_1 can be determined by assuming $z=0$. In this case $\dot{H}_m = A_1$, i.e. it has a given value on the surface of the superconductor.

It can therefore be written as:

$$A_1 = H e^{i\varphi_0} = \dot{H}_{m0}$$

Thus, the solution of equation (26) will be as follows:

$$\dot{H}_m = \dot{H}_{m0} e^{-pz} \quad (31)$$

Using the first equation in (25), we obtain an expression for the voltage of the electric field:

$$\dot{E}_m = \frac{1}{\sigma_N} p \dot{H}_{m0} e^{-pz} \quad (32)$$

The wave resistance of the superconducting film in its normal state can then be determined by taking the relation

of \dot{E}_m to \dot{H}_m :

$$Z_N = \frac{\dot{E}_m}{\dot{H}_m} = \frac{(1+i)}{\sigma_N} \sqrt{\frac{\omega\mu_0\sigma_N}{2}} = i\omega\mu_0 \frac{(1-i)}{2} \sqrt{\frac{2}{\omega\mu_0\sigma_N}} \quad (33)$$

or

$$Z_N = i\omega\mu_0\delta \quad (34)$$

$$\text{where } \delta = \frac{(1-i)}{2} \sqrt{\frac{2}{\omega\mu_0\sigma_N}}$$

or

$$\delta = \frac{(1-i)\delta_{sk}}{2} \quad (35)$$

This model is valid provided that the EMW frequency does not exceed the critical ω_{kp} value, which is determined by the connection energy of the charge carriers at $T < T_c$.

2) *The analysis of the HTS film parameters necessary for the implementation of the EMR protection device.*

If the film is part of an open transmission line, to define a surface film impedance the expression can be formed:

$$Z = \frac{i\omega\mu_0\delta}{\text{th}\left(\frac{h}{\delta}\right)} \quad (36)$$

Then, for a superconducting film, based on (20), let's determine the surface impedance:

$$Z = i\omega\mu_0\lambda_1 \left(1 - \frac{1}{2} i\omega\mu_0\sigma_N\lambda_1^2\right) F_S(x) \quad (37)$$

$$\text{where } F_S(x) = \frac{\text{sh}2x}{\text{ch}2x - 1}, \quad x = \frac{h}{\lambda_1}$$

h is the thickness of superconducting film.

It should be noted that if the thickness of superconducting film h is commensurate with the penetration depth λ_1 , then the film is partially transparent to EMWs, and such film is commonly referred to as thin film.

If we consider that if $h \gg \lambda_1$ $\text{sh}(2h/\lambda_1) \approx \text{ch}(2h/\lambda_1)$ $\gg 1$, and if $h \ll \lambda_1$ $\text{sh}(2h/\lambda_1)$ and $\text{ch}(2h/\lambda_1)$ are decomposed into power series, then we can obtain a reasonably accurate representation of $F_S(x)$ as [21]:

$$F_S(x) = \begin{cases} \frac{1}{x}, & x \leq 2, \\ 1, & x > 2. \end{cases} \quad (38)$$

The approximation error is maximum at $x=2$ and is 9%.

For the film in normal condition, in accordance with (35) we shall record:

$$Z_N = \frac{1}{2} \omega\mu_0\delta_{sk} (1+i) F_N(x) \quad (39)$$

where δ_{sk} is the thickness of the skin layer,

$$F_N(x) = \frac{\text{sh}2x - i\text{sin}2x}{\text{ch}2x - \text{cos}2x}, \quad x = \frac{h}{\delta_{sk}}$$

In this case we also obtain an approximation formula:

$$F_N(x) = \begin{cases} \frac{1-i}{2x}, & x \leq 1, \\ 1, & x > 1. \end{cases} \quad (40)$$

Error approximating reaches maximum value at $x=1$ and doesn't exceed 10%.

Let us record the final ratio for the active surface resistance R , which is the real part of the surface impedance, and the surface reactive resistance X , which is the imaginary part thereof, in superconducting and normal states:

$$R_S = \begin{cases} \frac{(\omega\mu_o)^2\sigma_N\lambda_1^4}{2h}, & h \leq 2\lambda_1 \\ \frac{1}{2}(\omega\mu_o)^2\sigma_N\lambda_1^3, & h > 2\lambda_1 \end{cases} \quad (41)$$

$$R_N = \begin{cases} (\sigma_N h)^{-1}, & h \leq \delta_{sk} \\ \frac{1}{2}\omega\mu_o\delta_{sk}, & h > \delta_{sk} \end{cases} \quad (42)$$

$$X_S = \begin{cases} \frac{\omega\mu_o\lambda_1^2}{h}, & h \leq 2\lambda_1 \\ \omega\mu_o\lambda_1, & h > 2\lambda_1 \end{cases} \quad (43)$$

$$X_N = \begin{cases} 0, & h \leq \delta_{sk} \\ \frac{1}{2}\omega\mu_o\delta_{sk}, & h > \delta_{sk} \end{cases} \quad (44)$$

If a superconducting film is used as the basis of a protective device (switch), having two stable states, superconducting and normal, then, in accordance with [22], enter a quality factor K :

$$K = \frac{(R_1 - R_2)^2 + (X_1 - X_2)^2}{R_1 R_2}, \quad (45)$$

$$K \gg 1,$$

where R_1, R_2, X_1, X_2 are the active and reactive components of the complete resistance of the protective device in two states (superconducting and normal).

This quality parameter is a universal characteristic of switched element in microwave circuits. If a superconducting strip is used as a switchable element capable of being in two states, the K -quality parameter is also its most important characteristic.

As a protective device, consider a superconducting film with length l , width W ($W < l$) and thickness h .

Then:

$$K = \frac{(R_N - R_S)^2 + (X_N - X_S)^2}{R_N R_S} = \quad (46)$$

$$= K_R + K_X.$$

It is obvious that. $R_S \ll R_N$

In addition, according to equations (41) to (44), K_X makes a significant contribution only in case of sufficiently thick ($h \geq \lambda_1$) superconductor films when K is below its maximum value. Then the quality parameter can be written as:

$$K \approx K_R = \frac{R_N}{R_S} = \frac{1}{2} \left(\frac{(\delta_{sk}/\lambda_1)^3 (F_N(h/\delta_{sk}))}{F_S(h/\lambda_1)} \right). \quad (47)$$

Using approximations (40) and (42), we obtain:

$$K_R = \begin{cases} \frac{1}{4}(\delta_{sk}/\lambda_1)^4, & h \leq 2\lambda_1 \ll \delta_{sk}; \\ \frac{1}{2}(\delta_{sk}/\lambda_1)^3(\delta_{sk}/h), & 2\lambda_1 \leq h \leq \delta_{sk}; \\ \frac{1}{2}(\delta_{sk}/\lambda_1)^3, & 2\lambda_1 \ll \delta_{sk} \leq h. \end{cases} \quad (48)$$

Thus, the highest value of the quality coefficient K_m is realized when the thickness of the film is less than or equals to penetration depth λ_1 :

$$K_m \approx K_{Rm} = \frac{1}{4}(\delta_{sk}/\lambda_1)^4. \quad (49)$$

In this case, when the film thickness h is reduced, R_N and R_S grow equally, so K_{Rm} does not depend on h .

However, it should be noted, that this dependence is only valid if the quality of the film is independent of h .

Films obtained in the real conditions of the existing technology contain defects and are not uniform in thickness. Therefore, by reaching K_{Rm} at $h \approx \lambda_1$, K_R can start to decrease at $h < \lambda_1$. The thickness of the film from which K_R becomes less than K_{Rm} characterizes the thickness of the defective layer.

IV. RESULTS AND DISCUSSION

At $T < T_c$, the HTS is at superconducting state. At $T > T_c$, the stripe has only normal conductivity. The superconducting state is destroyed provided that the frequency of the EMW does not exceed the critical value ω_{kp} , which is determined by the connection energy of the charge carriers at $T < T_c$. For HTS $\omega_{kp} = 10^{13} - 10^{14} \text{ c}^{-1}$, that is, it is much higher than the frequency of microwave range.

If the skin layer of the London-wide HTS penetration depth is significantly exceeded, the penetration of the EMW into the superconductor ceases to be frequency dependent and equals the London penetration depth. If the EMW falls on a flat boundary between the free space and the superconductor, and the thickness of the superconducting layer is much larger than the London penetration depth, the surface impedance becomes equal to its wave resistance. In such a case, the superconductor has high critical current values and cannot be used to protect the radio electronic media from a powerful EMR. To implement a protective device based on HTS, the thickness of the film must be consistent with the London penetration depth. In doing so, it is necessary to take into consideration the possible irregularities and defects of the film in order to ensure that the condition of equality of film thickness and penetration depth is met.

Further studies of the use of superconducting films, according to the authors, should be primarily aimed at solving the following priority problems:

1. Investigation of the effectiveness of protective devices based on superconducting films.
2. Development of options for constructing superconducting protective devices based on strip transmission lines.
3. Study of the influence of superconducting protective devices on the passage of working signals.
4. Study of the influence of superconducting protective devices on the passage of powerful electromagnetic pulses through the antenna-feeder path of the receiving device.

V. CONCLUSION

1. As a result of studies of the propagation of EMW over the surface of a thin HTS, the basic relations were obtained for determining the value of the surface impedance and the depth of penetration of EMW into a superconducting film in the superconducting S and normal N states. It is shown that the expression for determining the penetration depth of EMW into a superconducting film in the normal N state is applicable provided that the frequency of the signal field does not exceed the critical value, which is determined by the binding energy of charge carriers at a temperature not exceeding the transition temperature to the superconducting state.
2. As a result of the analysis of the HTS film parameters required for the implementation of the EMR protection device, a correlation of the HTS on film thickness It is shown that the highest value of the quality coefficient is realized when the thickness of the film is less than or equals the penetration depth. It has been established that this dependence is only valid if the thickness of the film is independent of its quality.

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